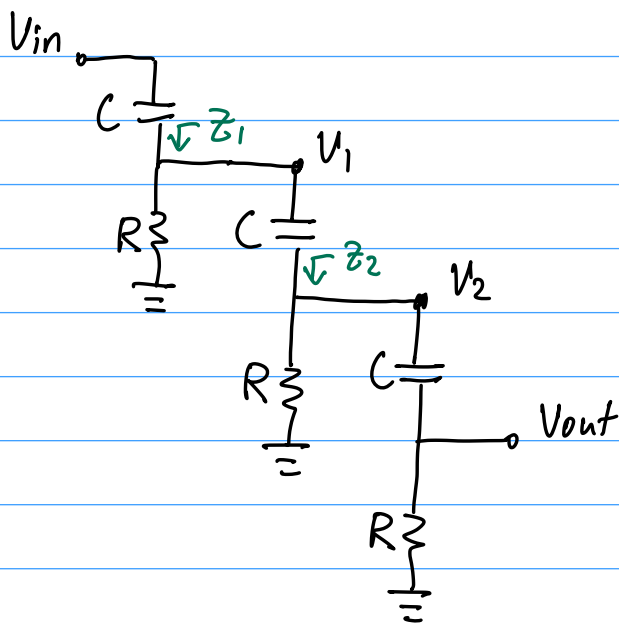


Redraw as a cascade of voltage dividers.



$$\begin{aligned} Z_2 &= R \parallel \left(\frac{1}{sC} + R \right) \\ &= \frac{\frac{R}{sC} + R^2}{\frac{1}{sC} + 2R} \\ &= \frac{R + sR^2C}{1 + 2sRC} \end{aligned}$$

$$\begin{aligned} Z_1 &= R \parallel \left(\frac{1}{sC} + Z_2 \right) \\ &= \frac{\frac{R}{sC} + RZ_2}{\frac{1}{sC} + R + Z_2} \\ &= \frac{R + sRCZ_2}{1 + sRC + sCZ_2} \end{aligned}$$

Next write voltage divider expressions.

$$V_1 = V_{in} \frac{Z_1}{\frac{1}{sC} + Z_1} = \frac{V_{in} sC Z_1}{1 + sC Z_1}$$

$$V_2 = \frac{V_1 Z_2}{\frac{1}{sC} + Z_2} = \frac{V_1 sC Z_2}{1 + sC Z_2} = V_{in} \left(\frac{sC Z_1}{1 + sC Z_1} \right) \left(\frac{sC Z_2}{1 + sC Z_2} \right)$$

$$V_{out} = \frac{V_2 R}{\frac{1}{sC} + R} = \frac{V_2 sCR}{1 + sCR}$$

$$\frac{V_{out}}{V_{in}} = \left(\frac{sC Z_1}{1 + sC Z_1} \right) \left(\frac{sC Z_2}{1 + sC Z_2} \right) \left(\frac{sCR}{1 + sCR} \right)$$

Now use a computer algebra system!

syms s R C Vin

$$Z2 = (R + s*R^2*C) / (1 + 2*s*R*C);$$

$$Z1 = (R + s*R*C*Z2) / (1 + s*R*C + s*C*Z2);$$

$$H = \text{simplify}((s*C*Z1)/(1 + s*C*Z1) * (s*C*Z2)/(1 + s*C*Z2) * (s*C*R)/(1 + s*C*R))$$

H =

$$\frac{C^3 R^3 s^3}{C^3 R^3 s^3 + 6 C^2 R^2 s^2 + 5 C R s + 1}$$