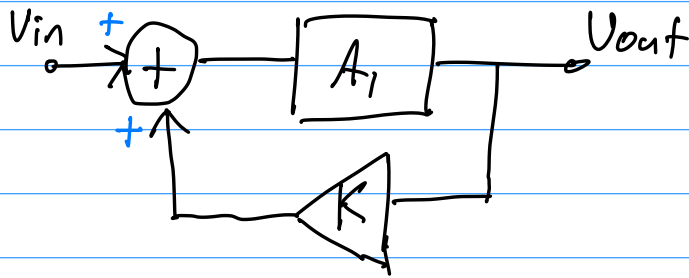


Each stage has a transfer function

$$H_1(s) = \frac{-g_m R_D}{1 + \frac{s}{\omega_p}}$$

where  $\omega_p = \frac{1}{R_D C}$ .

$\therefore$  The open loop amp. has  $A_1 = -\frac{(g_m R_D)^3}{(1 + \frac{s}{\omega_p})^3}$ .



$A_1$  is negative  $\therefore$  Neg. feedback requires a + at the adder.

$\therefore$  Loop gain =  $-KA_1$ .

$\therefore$  Loop gain  $T = -KA_1 = +\frac{(g_m R_D)^3}{(1 + \frac{s}{\omega_p})^3}$ .

Subst  $s = j\omega$ ,  $\omega_p = \frac{1}{R_D C}$  and set  $T = -1$ .

$$\frac{(g_m R_D)^3}{(1 + j\omega R_D C)^3} = -1$$

$$\begin{aligned} - (g_m R_D)^3 &= (1 + j\omega R_D C)^3 \\ &= (1 + j\omega R_D C)(1 + 2j\omega R_D C - \omega^2 R_D^2 C^2) \\ &= 1 + 2j\omega R_D C - \omega^2 R_D^2 C^2 + j\omega R_D C \\ &\quad - 2\omega^2 R_D^2 C^2 - j\omega^3 R_D^3 C^3 \\ &= 1 + 3j\omega R_D C - 3\omega^2 R_D^2 C^2 - j\omega^3 R_D^3 C^3. \end{aligned}$$

LHS is real  $\therefore$  RHS is real.  $\therefore$  Take imag. part = 0.

$$3\omega R_D C - \omega^3 R_D^3 C^3 = 0$$

$$3 - \omega^2 R_D^2 C^2 = 0$$

$$\therefore \omega^2 = \frac{3}{R_D^2 C^2}$$

$$\therefore f_{osc} = \frac{\sqrt{3}}{2\pi R_D C}$$